

Clicker question

You are tasked with measuring the height of a tree and you get the measurement as 170 ft tall. You later realized that your measurement tools are somewhat faulty, up to a relative error of 10%. What is the minimum height of the tree (numbers rounded to 3 sig figs) ?

A) 153 ft

B) 155 ft

C) 187 ft

D) 189 ft

$$\hat{x} = 170 \text{ ft}$$

$$e_r = 0.1$$

$$e_r = \frac{|x - \hat{x}|}{|x|} \rightarrow e_r x = |x - \hat{x}|$$

$$\begin{cases} \hat{x} = x(1 - e_r) \\ \hat{x} = x(1 + e_r) \end{cases}$$

$$x = \frac{\hat{x}}{(1 - e_r)} \quad \text{or} \quad x = \frac{\hat{x}}{(1 + e_r)}$$

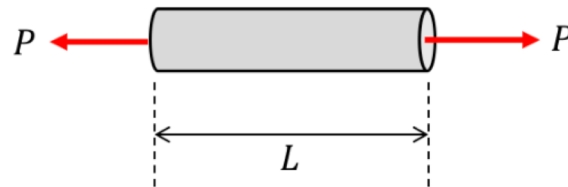
$$x = \frac{170}{1.1} = 154.545$$

$$x = 155 \text{ ft}$$

For the circular rod below, we can determine the change in the length L as

$$\delta = \frac{FL}{EA}$$

where $F = 38 \times 10^3 \text{ N}$ is the force, $L = 1 \text{ m}$ is the length of the bar, $A = 19 \times 10^{-6} \text{ m}^2$ is the circular cross section area, and $E = 105 \times 10^9 \text{ N/m}^2$ is a material property.



What is the value of δ ?

$\delta =$ m

Select all of the options that will give you the correct answer above

- A) 0.01904761904761905
- B) 0.019
- C) 0.0190
- D) 0.01905
- E) 0.019048

$rtol = 10^{-3}$

relative error

$$e_r \leq 10^{-3} = 10^{-n+1}$$

| hence $n=4$ |

the approximated answers should have at least 4 significant digits!

Clicker question

Matrix Norm Approximation

Suppose you know that for a given matrix A three vectors \mathbf{x} , \mathbf{y} , \mathbf{z} for the vector norm $\|\cdot\|$,

$$\|\mathbf{x}\| = 2, \|\mathbf{y}\| = 1, \|\mathbf{z}\| = 3,$$

and for corresponding induced matrix norm,

$$\|A\mathbf{x}\| = 20, \|A\mathbf{y}\| = 5, \|A\mathbf{z}\| = 90.$$

What is the largest lower bound for $\|A\|$ that you can derive from these values?

a) 90

b) 30

c) 20

d) 10

e) 5

$$\|A\|_p = \max \left\{ \frac{\|A\mathbf{x}\|}{\|\mathbf{x}\|}, \frac{\|A\mathbf{y}\|}{\|\mathbf{y}\|}, \frac{\|A\mathbf{z}\|}{\|\mathbf{z}\|} \right\}$$

$$= \max \{ 10, 5, 30 \} = 30$$

Clicker question

Suppose you have $A = U \Sigma V^T$ calculated. What is the cost of solving

$$\min_x \|b - Ax\|_2^2 \quad x = V \sum_R^T U_R^T b$$

A) $O(n)$

B) $O(n^2)$

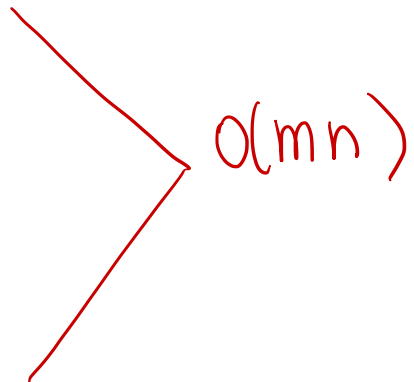
C) $O(mn)$

~~D) $O(m)$~~

E) $O(m^2)$

$$z = U_R^T b = \begin{bmatrix} u_1^T b \\ u_2^T b \\ \vdots \\ u_n^T b \end{bmatrix} \begin{matrix} O(m) \\ \\ \\ O(m) \end{matrix}$$

$n \times m$ $m \times 1$



$$y = \sum_R^T z = \begin{bmatrix} \cdot & & \\ & \cdot & \\ & & \cdot \end{bmatrix} \begin{bmatrix} z \\ \\ \\ \end{bmatrix} = 0 \rightarrow O(n) \text{ diagonal !!}$$

$n \times n$ $n \times 1$

$$x = Vy = \begin{bmatrix} v_1 & v_2 & \dots & v_n \end{bmatrix} \begin{bmatrix} y_1 \\ \vdots \\ y_n \end{bmatrix} \rightarrow O(n^2)$$

since $m > n$
 $O(mn)$

Clicker question

Mark the incorrect statement about the Bisection Method:

- A) Has linear convergence *True*
- B) Requires two function evaluations for each iteration, i.e. $f(a)$ and $f(b)$ *False*
- C) The function must be continuous with a root in the interval $[a, b]$ *True*
- D) Given the initial interval $[a, b]$, the length of the interval after k iterations is $\frac{b-a}{2^k}$ *True*

→ only at first iteration we have two function evaluations, then only one function evaluation per iteration is needed.

CONTINUE DEMO